



JAYOTI VIDYAPEETH WOMEN'S UNIVERSITY, JAIPUR  
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**Faculty of Education and methodology**

**Department of Science and Technology**

**Faculty Name-** Jv'n Narendra Kumar Chahar (Assistant Professor)

**Program-** B.Tech 8<sup>th</sup>Semester

**Course Name-** Cryptography and Network Security

**Session no.:** 21

**Session Name-** Multi-Precision Arithmetic

Academic Day starts with –

- Greeting with saying '**Namaste**' by joining Hands together following by 2-3 Minutes Happy session, Celebrating birthday of any student of respective class and **National Anthem**.

Lecture starts with- quotations' answer writing

Review of previous Session – **RSA public key cryptosystem**

Topic to be discussed today- Today We will discuss about **Multi-Precision Arithmetic**

Lesson deliverance (ICT, Diagrams & Live Example)-

- Diagrams

Introduction & Brief Discussion about the Topic- **Multi-Precision Arithmetic**

## Multi-Precision Arithmetic

This involves libraries of functions that work on multiword (multiple precision) numbers and multiplication digit by digit. Also, it does exponentiation using square and multiply are a number of well-known multiple precision libraries available - so don't reinvent the wheel.

We can use special tricks when doing modulo arithmetic, especially with the modulo reductions

### **Faster Modulo Reduction**

Chivers (1984) noted a fast way of performing modulo reductions whilst doing multi-precision arithmetic calcs.

Given an integer A of n characters ( $a_0, \dots, a_{n-1}$ ) of base b

$$A = \sum_{i=0}^{n-1} a_i b^i$$

then

$$A \equiv \left\{ \sum_{i=0}^{n-2} a_i b^i + a_{n-1} b^{n-1} \pmod{jm} \right\} \pmod{m}$$

ie: this implies that the MSD of a number can be removed and its remainder mod m added to the remaining digits will result in a number that is congruent mod m to the original.

\* Chivers algorithm for reducing a number is thus:

Construct an array  $R = (bd, 2.bd, \dots, (b-1).bd) \pmod{m}$

FOR  $i = n-1$  to  $d$  do

WHILE  $A[i] \neq 0$  do

$j = A[i];$

$A[i] = 0;$

$A = A + b_i \cdot d \cdot R[j];$

END WHILE

END FOR

where  $A[i]$  is the  $i$ th character of number  $A$   $R[j]$  is the  $j$ th integer residue from the array  $R$   $n$  is the number of symbols in  $A$ ,  $d$  is the number of symbols in the modulus

### **Speeding up RSA - Alternate Multiplication Techniques**

- conventional multiplication takes  $O(n^2)$  bit operations, faster techniques include the Schönhage-Strassen Integer Multiplication Algorithm:
- breaks each integer into blocks, and uses them as coefficients of a polynomial
- evaluates these polynomials at suitable points, & multiplies the resultant values
- interpolates these values to form the coefficients of the product polynomial
- combines the coefficients to form the product of the original integer
- the Discrete Fourier Transform, and the Convolution Theorem are used to speed up the interpolation stage
- can multiply in  $O(n \log n)$  bit operations

the use of specialized hardware because:

- conventional arithmetic units don't scale up, due to carry propagation delays
- so can use serial-parallel carry-save, or delayed carry-save techniques with  $O(n)$  gates to multiply in  $O(n)$  bit operations, or can use parallel-parallel techniques with  $O(n^2)$  gates to multiply in  $O(\log n)$  bit operations

## **Reference-**

- 1. Book:** William Stallings, “Cryptography & Network Security”, Pearson Education, 4th Edition 2006.

## **QUESTIONS: -**

### **Q1. Explain Multi-Precision Arithmetic.**

Next, we will discuss more about RSA and the Chinese Remainder Theorem.

- Academic Day ends with-  
National song ‘Vande Mataram’